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$$x = (\frac{1}{2}a + \frac{1}{4}a)\cos\theta - (\frac{1}{4}a)\cos[(\frac{1}{2}a + \frac{1}{4}a)/(\frac{1}{4}a)]\theta,$$

and 
$$y = (\frac{1}{2}a + \frac{1}{4}a)\sin\theta - (\frac{1}{4}a)\sin[(\frac{1}{2}a + \frac{1}{4}a)/(\frac{1}{4}a)]\theta$$
.

These are the well-known equations of an epicycloid, the radii of the fixed and rolling circles being  $\frac{1}{2}a$  and  $\frac{1}{4}a$  respectively.

B. The following geometrical solution is very much like one given in Wood's Optics, and was suggested by it.

Referring to the same figure, erect at P a perpendicular to CB, meeting OB at E. Comparing the similar triangles EPB and ODB, ED:DB=BP:BD=1:2.

If, then, upon EB, the half of OB, as diameter, a circumference be drawn its intersection with CB will be a point of the caustic. With O as center and EO as radius describe a semi-circle, intersecting the X-axis at K.

The  $\angle EOK = \theta$ , and arc  $EK = \frac{1}{2}a\theta$ .

Also, since  $\angle EBP = \theta$ , the angle at the center measured by arc  $EP = 2\theta$ ; and arc  $EP = \frac{1}{2}a \cdot 2\theta = \frac{1}{2}a \cdot \theta$ .

Hence arc EP=arc EK.

The locus of P is, therefore, generated by the circle EPB rolling on the circle EK, the points P and K being originally in contact.

Of course the problem may be solved without assuming the property quoted from *Price*. In *Rice and Johnson's Differential Calculus* an excellent solution is outlined.

Also solved by C. W. M. BLACK, S. H. WRIGHT, and B. F. FINKEL.

### PROBLEMS FOR SOLUTION.

## ARITHMETIC.

- 97. Proposed by J. A. CALDERHEAD, M. Sc., Professor of Mathematics. Curry University, Pittsburg, Pa. In what time will \$4000 amount to \$5134.96, interest at 6% payable annually?
- \*\* Solutions of these problems should be sent to B. F. Finkel, not later than July 10.

#### GEOMETRY.

#### 97. Proposed by CHAS. C. CROSS, Libertytown, Md.

Prove by pure geometry: The radius of a circle drawn through the centers of the inscribed and any two escribed circles of a triangle is double the radius of the circumscribed circle of the triangle.

98. Proposed by EDW. R. ROBBINS, Master in Mathematics and Physics, Lawrenceville School, Lawrenceville, N. J.

Construct a circle which shall pass through two given points and touch a given circle, (1) when the distance between the points is less than the diameter of the circle, and (2) when it is greater.

\*\* Solutions of these problems should be sent to B. F. Finkel, not later than July 10.